

New Holes and Boundary Detection Algorithm for Heterogeneous Wireless Sensor Networks

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Abstract: Hole is an area in wireless sensor network (WSN) around which nodes cease to sense or communicate due to drainage of battery or any fault, either temporary or permanent. Holes impair sensing and communication functions of network; thus their identification is a major concern. In this paper, a distributed solution is proposed for detecting boundaries and holes in the WSN using only the nodes connectivity information and estimated distance between nodes. Our protocol is divided into four main phases. In the first phase, each node discovers its coverage neighbors and collects their information. In the second phase, each node communicates with its neighbors to find whether its sensing range is fully covered by the sensing ranges of its neighbors. In the third phase, the boundary nodes connect with each other to complete the boundary information. In the fourth phase, a boundary sub-graph amongst boundary nodes is constructed and classified either as an interior or an exterior boundary. Simulation results show that our approach improves the energy and reduces the number of boundary nodes over existing algorithms.

Keywords: Arbitrary sensing ranges, Coverage holes, Boundary detection, Distributed algorithm, Un-localized sensors.

1. Introduction

WSN is a network composed of a large number of nodes by means of self-organization and multi-hops. WSNs have myriad of interdisciplinary applications such as weather forecasting, battlefield surveillance, threat identification, health monitoring and environment monitoring [1, 14]. All those applications that demand random deployment and uncontrolled environment suffer from holes problem. Hole detection is one of the major problems in WSN. Holes affect the network capacity and perceptual coverage of the network. Due to limited battery the nodes may die with passage of time. In case of random deployment, there is a huge possibility that all areas of target region are not covered properly leading to formation of holes. Detection of holes is important because of their negative and damaging effects. If there is a hole in the network then data will be routed along the hole boundary nodes again and again which will lead to premature exhaustion of energy present at these nodes. This will ultimately increase the size of hole in the network. Detection of holes avoids the additional energy consumption around holes because of congestion. We detect the hole in WSNs through detection of hole boundary, that is, the nodes that are present on the hole boundary. Whether a node is an inner or a boundary might be crucial for object tracking scenarios. For example, when tracking events entering and leaving a region, boundary nodes might be involved in more complex sensing tasks whereas inner nodes might spend more energy on satisfying routing tasks. Most applications and research works focus on homogeneous WSNs, where all nodes are identical in terms of energy resources, computation and wireless communication capabilities. However, the assumptions that all the nodes have the same sensing or

communication ranges might not be accurate. To overcome these problems, heterogeneous WSNs consisting of two or more different types of nodes: the high-end ones have higher processing throughput and longer communication / sensing range; the low-end ones are much cheaper and with limited computation and communication / sensing abilities. A mixed deployment of these nodes can achieve a balance of performance and cost of a WSN. Numerous real life examples using a large scale WSN use heterogeneous nodes. In this paper, using only estimated distance between nodes, 1- and 2-hops, we present a scalable solution that recognizes both the inner and boundary nodes in a two-dimensional space with heterogeneous sensing range. Our approach sets no constraints on the node distribution and the node density. In addition, we propose two distributed algorithms to characterize some global properties of the boundaries. The rest of the paper is organized as follows: In Section 2, we describe the related work of our problem. The problem assumption, definitions and the proposed algorithm with a step by step description is given in Section 3. The simulation of our algorithm is presented in Section 4. Section 5 concludes our work.

2. Related Work

There has been a large body of research on detection of coverage holes in WSNs over the last few years. Coverage hole detection algorithms have been divided into three approaches, namely, topological, statistical, and geographical approaches [15]. Geographical Approach: This approach assumes that exact location of sensor nodes is known beforehand. Each node knows its location either with the help of special location hardware such as GPS [16] or by using scanning devices, thereby increasing size and structure of sensor nodes. It is also known as location based approach. In [17], the authors proposed a hole detection and adaptive geographical routing (HDAR) algorithm to detect holes and to use this information to deal with local minimum problem. If the angle between two adjacent edges of a node is greater than 120 degrees, then it begins hole detection algorithm. Statistical Approach: Some statistical function is applied on data collected from neigh-boring nodes and then a Boolean function decides whether nodes are at hole boundary or not. It is based on the assumption that distribution of nodes follows some statistical function. There is no need of GPS, but it requires high node density; that is, average degree must be 100 or higher [18]. In practice, such dense uniform deployment is not practical. The concept used in [18] is that boundary nodes have lower average degrees than interior nodes. Average density is the metric used to detect holes where actual node degree is compared with a pre-defined threshold value to infer its position. Another metric used in

[18] is centrality index, where high value is assigned to inner nodes and less value to outer nodes. We have considered many algorithms under different categories each having its own limitations. Geometrical approach for hole detection requires GPS enabled sensors and is expensive. They consume a lot of energy and it is not practical for sensors to know their exact location in hostile environment. Considering huge applications of WSN, these approaches have limited scope. Statistical approaches provide optimal performance, but they are computationally expensive. Owing to the challenges in wireless sensor networks it is not desirable that nodes perform complex mathematical and statistical calculations [15]. Topological approach provides realistic results but involves communication overhead. Some of the algorithms do not work for small network degrees.

Topological Approach: Also called as connectivity based approach, it uses only the available connectivity information of network to detect holes. This approach requires no location information and works even for dense networks. There is no assumption about node distribution. One of the algorithms based on topological approach to detect coverage holes within WSNs was given in [19] and later improved in [20]. Authors proposed a distributed cooperative scheme based on the fact that nodes at the hole or network boundary have smaller degrees than interior nodes. It deals with static, uniformly distributed nodes with each node having a unique id. If the degree of a node is lower than the average degree of its 2-hop neighbors, then it makes a decision whether it is on hole boundary or not. If yes, then it sends messages informing its status to its 1-hop neighbors who may also be on hole boundary. The algorithm is scalable, but approach produces poor results for randomly deployed dense networks. If there are not sufficient nodes surrounding a hole then output produced is not accurate. In [21], the authors used the concepts of Rips complex and Cech complex to discover coverage holes. If communication radius is greater than or equal to twice the sensing radius and there is a hole in Rips complex, then there must be a hole in Cech complex. The distributed algorithm proposed by authors is capable of detecting non triangular holes and the area of triangular holes. After constructing neighbor graph, each node checks whether there exists a Hamiltonian cycle in graph. If not, then node is on the hole boundary. After making decision, each node broadcasts its status to its neighbors. The algorithm further finds cycles bounding holes. In [22], the authors proposed a hop based approach to find holes in sensor networks. There are three phases, namely, information collection phase where each node exchanges information to build a list of x-hop neighbors, path construction phase where communication links between sensor nodes in list of x-hop neighbors are identified, and finally path checking phase where paths are examined to infer boundary and inner nodes. If the communication path of x-hop neighbors of a node is broken, then it is a boundary node. Algorithm works for node degree of 7 or higher which is better than some of the other approaches, but there is a huge communication overhead involved identifying x-hop neighbors. In [23], the authors proposed decentralized boundary detection (DBD) algorithm to identify sensor nodes near a hole or obstacle in WSN using topological approach. Each node knows its three-hop neighbors by exchanging HELLO messages and 1-hop and 2-hop node information. There is no UDG constraint. Each node then constructs 2-hop neighbor graph. If cycle exists in such a graph, then there is a hole in

network. For dealing with hole which is not included totally inside 2-hop neighbor graph, another rule based on contour structure was developed. Detection of broken contour line implies either network boundary or an obstacle. There are very few algorithms that can detect boundaries of small holes. In [24], the authors proposed a distributed algorithm that can accurately detect boundaries of small holes in the network. The first step of algorithm is to reduce the connectivity graph by using vertex deletion and edge deletion so as to obtain a skeleton graph. Thereafter, skeleton graph is further partitioned to get coarse inner boundary cycles. Each cycle either encloses a hole of graph or corresponds to outer boundary. The coarse outer boundaries are then further refined to get fine grained boundary cycles. There is no assumption related to node density. The authors further proved the correctness of hole detection.

Our proposed algorithm belongs to the third category where, without network synchronization and position information and using only 1- and 2-hops, we present a scalable algorithm that recognizes both the inner and boundary nodes in a two-dimensional space with heterogeneous sensing range. Our approach sets no constraints on the node distribution and the node density. It uses unit disk graph for the communication range. The proposed algorithm not only reduces the consumed energy but also minimizes the number of nodes that cover the network boundary. Our algorithm can precisely identify the boundary nodes, even in a sparsely deployed environment. The local boundary classifications are used to create a boundary sub-graph and to determine if a boundary sensor node is located on a hole or on the outer boundary of the network.

3. Boundary and Hole Detection Algorithm

In this section, we start by giving the problem assumptions and the key definitions regarding the field and the nodes.

3.1 Problem Assumptions

Our approach relies on the following key assumptions regarding the field and the nodes:

- All sensor nodes are randomly deployed in a monitoring region and some irregular holes may exist.
- Each sensor node has a unique ID.
- The sensor nodes have sensing ranges that are different from their communication ranges ($R_c \geq R_s$).
- Every sensor node can estimate the distances from its 1-hop neighbors using RSSI.

3.2 Definitions and Notations

We assume that there are randomly scattered n heterogeneous sensor nodes over a monitored area form the set V , where $V = \{v_i : i = 1, \dots, n\}$ such that $R_c \geq R_s$.

Definition 1: A node v is a boundary node if there is a point p on the sensing region of $v(C(v))$ such that p is not covered by the sensing range of any other node.

Definition 2: The shared edge between v and u where $u \in C(v)$ is the cross edge between the intersection of $C(v)$ and $C(u)$. The shared edges of node $v(SE(v))$ is the set of all shared edges between v and the nodes of coverage neighbor ($CN(v)$). $SE(v) = \{v_i v_j : \text{where } v_i v_j \text{ is a shared edge between } v \text{ and a node in } CN(v)\}$.

Definition 3: A coverage polygon of a node $v(P(v))$ is the set of vertices that result from the intersection of edges

in $SE(v)$. $P(v)$ is bounded if the number of shared edges equals to the number of vertices.

Here, we outline our proposed algorithm for discovering the hole and its boundary of an un-localized heterogeneous WSN.

The algorithm includes four phases: initial, discovery and detection, selection and connection, and classification.

In the first initial phase, each node discovers its coverage neighbors and collects their information. In the second discovery and detection phase, each node communicates with its neighbors to find whether its sensing range is fully covered by the sensing ranges of its neighbors. In the selection and connection phase, the boundary nodes connect with each other to complete the boundary information. In the classification phase, a boundary sub-graph amongst boundary nodes is constructed and classified either as an interior or an exterior boundary.

Here in the following phases, we use two relevant procedures: (1) 1-hop sorting to sort the 1-hop neighbors of a node according to a randomly selected neighbor and (2) 2-hops Distance to characterize connectivity pattern by computing the distance between a node and any other node in its 2-hops neighbors [5].

3.3 Initial Phase: Boundary Coverage Neighbors Discovery

Lemma: The sensing range of any node can be completely covered by its $N(v)$ and $N(v)$.

Proof: Assume that a sensor node v is covered by a sensor node x and $x \in N_3(v)$ i.e., $x \notin N_1(v)$ and $x \notin N_2(v)$.

If v and x have maximum sensing range, i.e., $R_s = R_c$, then $C(x) \cap C(v) \neq \emptyset$ and so $dvx \leq 2 * R_c$ which induces a contradiction that implies the sensing range of x does not intersect with the sensing range of v .

In this phase, each node discovers its coverage neighbors and collects their information [5].

3.4 Boundary detection phase

In this phase, every node uses its BC set to detect if it is a boundary or an inner node in the network by executing the following procedure:

1. If your sensing range is fully covered by one node, then declare yourself as an inner node.
2. Otherwise, using a subset of $BC(v)$ ($Sub - Neigh(v)$), construct $P(v)$ (we use only a subset of BC to reduce the computation complexity of high density networks). The selection of $Sub - Neigh(v)$ will be as follows:

Case 1: select four nodes in four different directions to construct $Sub - Neigh(v)$ as follows:

- Select a random node $u \in BC(v)$ and add v to $Sub - Neigh(v)$.
- For each node $\in BC(v)$ do
 1. Select w , such that $\pi/2 < \angle uvw < \pi$ and add w to $Sub - Neigh(v)$.
 2. Select x , such that $\pi < \angle uvx < 3\pi/2$ and add x to $Sub - Neigh(v)$.
 3. Select y , such that $3\pi/2 < \angle uvy < 2\pi$ and add y to $Sub - Neigh(v)$.

If v cannot create $Sub - Neigh(v)$ in case 1, it will try one of the following two cases.

Case 2: select 3 nodes in three different directions using previous procedure.

Case 3: select two nodes in two different directions using previous procedure and then select cross node between them such that the angle between the cross node and every selected node should be more than or equal to 45° .

3. Using $Sub - Neigh(v)$, construct $P(v)$ by constructing $SE(v)$.
4. Run the *Bounded Test* to check the boundedness of the constructed $P(v)$.
 - a. If every two adjacent shared edges in $SE(v)$ are intersected, then $P(v)$ is bounded and therefore, start the covered test.
 - b. Otherwise, while unbounded $P(v)$ or there is an unselected node in $BC(v)$.
 - i. Find a new node in $BC(v)$ that is close to the unbounded area of $P(v)$ (between the two adjacent nodes that do not have shared edge).
 - ii. Add the new selected node to $Sub - Neigh(v)$, then reconstruct a new $P(v)$ based on the new $Sub - Neigh(v)$ and check the boundedness of the new $P(v)$.
 - c. If bounded $P(v)$, start the covered test.
 - d. Otherwise, declare yourself as a boundary node.

Note that the bounded test is not enough to decide the inner nodes because some nodes can pass the bounded test although they are not inner nodes.

Lemma: Every node v is a boundary node, if it has unbounded $P(v)$.

Proof: obvious from the bounded test definition.

In the next step, we study the coverage test to decide if the nodes with bounded $P(v)$ are inner or boundary nodes.

5. Run *Coverage Test*: Every node v has bounded $P(v)$ and will execute the coverage test as follows:

If the vertices of $P(v)$ are covered by the sensing range of v (covered $P(v)$), declare yourself as an inner node.

Otherwise, for every uncovered vertex $v \in P(v)$ execute the following procedure:

- a. while there is uncovered vertex $v \in P(v)$ and there is no more node in $BC(v)$ to be selected, do
 - i. Find node $w \in BC(v)$ such that w is close to v , and located between the two nodes say p, q that failed to form a covered vertex v .
 - ii. Add w to $Sub - Neigh(v)$, and construct the new $P(v)$.
 - iii. If the new $P(v)$ is covered, check the next uncovered vertex of $P(v)$.
 - iv. Otherwise, delete w from $Sub - Neigh(v)$ and find another node in $BC(v)$.

- b. If still there are uncovered vertices of $P(v)$, do the following:
- i. while there is uncovered $v \in P(v)$ or there is unselected node in $BC(v)$ do
 - A. Increase the width around v by finding node w in $BC(v)$ such that w located between two nodes r and s and r is the previous node to p and s is the next node to q in $Sub - Neigh(v)$ and $C(w)$ intersects with $C(r)$ and $C(q)$ or, with $C(p)$ and $C(s)$.
 - B. If there is w satisfies the previous conditions, add w to $Sub - Neigh(v)$.
 - C. Otherwise, select two nodes from $BC(v)$ such that they are located between r and s and satisfy the following conditions:
 - The sensing ranges of the two selected nodes are intersected.
 - The sensing range of r intersects with the sensing range of one of the two selected nodes and the sensing range of s intersects with the other node.
 - D. Check the new constructed $P(v)$.
 - c. If all vertices of $P(v)$ are covered, declare yourself as an inner node. Otherwise, declare yourself as a boundary node.

Lemma: If a node v has uncovered $P(v)$, then v is a boundary node.

Proof: Assume that $P(v)$ is not fully covered by the sensing range of v , i.e., there exists $v \in P(v)$, such that $v \nu > Rs(v)$, i.e., there is an arc of $C(v)$ which is not covered by the sensing ranges of the nodes forming v . Therefore, $C(v)$ is not fully covered by its boundary coverage neighbors.

In the boundary detection phase, each node directly declares itself as a boundary if its $P(v)$ is unbounded or bounded but uncovered by its neighbors. The boundary node announces its decision to its neighbors and then runs the Selection phase, where each boundary node will be connected with two boundary nodes in two different directions to complete its boundary information.

3.5 Selection and Connection Phase

Every boundary node v may receive several boundary declaration messages from its neighbor boundary nodes to complete its boundary neighbors list by executing the following procedure:

- Broadcast *Boundary Query message* to your neighbors with your *ID*.
- If you receive *Boundary Answer messages* from your neighbors, select the node u with the largest sensing range and smallest vertical distance, and

send *Candidate-Node* a reply message to be the new selected boundary node.

- Any node u that receives a *Boundary Query message* from v will execute the following procedure:

- From your neighbor list, find a boundary node w such that w and v are located in two different directions, i.e., $duw < dwv$ and $duv < dwv$.
- Send *Boundary Answer message* containing (your *ID*, dwv , *ID* of the selected boundary node) to v , and then wait for *Candidate Node* message reply.

After executing the selection phase, every boundary node v will have at least two boundary nodes in its boundary neighbor list. Then, v will start the connection phase by executing the following procedure:

- If the following conditions are satisfied:
 - for any two boundary nodes w and u , $dvw < duw$ and $dvw < duw$, and,
 - there is an overlap between the sensing range of v and the sensing ranges of w and u .
- Then, consider w and u as your forward boundary nodes, otherwise, go back to the selection phase.

3.6 Classification Phase

After each boundary node determines its boundary neighbors list, it uses a broadcast tree leader-election algorithm [27], but with the scope of the messages limited to only boundary nodes. The boundary node in the boundary sub-graph with the lowest ID becomes the root, and this ID is transmitted to all the other boundary nodes in the same boundary sub-graph. Each boundary node (child) in the sub-graph sends its vertical distance to its parent towards the root. Every boundary node w will have one of the following two cases:

Receiving only one root.ID message

If the received root.ID $>$ is your root.ID, then broadcast (your ID, root.ID) to your boundary node neighbors.

Otherwise, update your root.ID, and send (your ID, root.ID) to your boundary nodes that are not members of your boundary sub-graph (children).

Receiving more than one root.ID message

If all messages contain the same root.ID,

You are the end node of a boundary sub-graph.

Send (your ID, distance between you and your parents, root.ID) to your parents.

Otherwise, if all messages contain different root IDs and you are the end node of a boundary sub-graph,

You are a member in more than one sub-graph.

Update the root.ID to the smallest one of the received messages, and send (your ID, root.ID) to your boundary nodes (children) that are not members of your boundary sub-graph.

Otherwise, update root.ID to the smallest one of the received messages and send a message (your ID, root.ID) indicating that they are not members of your boundary sub-graph.

After a period of time, the boundary sub-graph root receives the length of its boundary sub-graph. If each node in the network knows the value of boundary of the network, then each boundary sub-graph root compares the value of the perimeter to the value of perimeter of the network and

determines if there is a hole inside the network or it actually represents the outer boundary of the network. The root of the sub-graph then rebroadcasts the results back to the sub-graph.

4. Simulation Results

A simulator has been implemented using ns-2 to estimate the performance of our proposed boundary nodes detection algorithm. Sensor nodes are randomly deployed in the monitoring region. The average node degree of the network is varied from 6 and 23 with an incremental step 4 by changing the sensing radius. The sensing ranges of sensor nodes are heterogeneous and increase with the average node degree of the network. In order to study the performance of our approach, we considered the following performance metrics:

Number of Boundary Nodes: is the number of boundary nodes in the network.

Communication Overhead: is measured by the total number of messages used in discovering boundary sensor nodes and connecting them in sub-graphs.

Energy Consumption: is measured by the total consumed energy in discovering boundary sensor nodes and connecting them in sub-graphs.

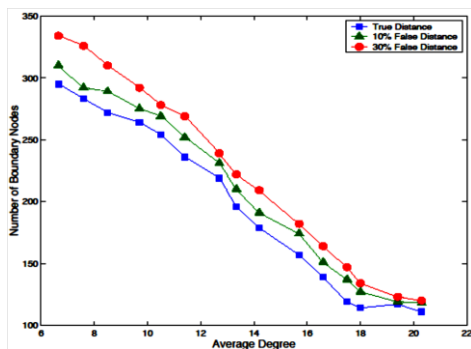


Figure 1. Number of boundary nodes under faulty distances vs. average node degrees.

In the first test, we consider the number of boundary nodes according to three different measurements: the true distance, the 10% faulty distance, and the 30% faulty distance. As expected, Figure 1a shows that the results of faulty distance are not as good as the true distance, especially in low average degree. This is because every sensor node in the network of our algorithm depends on its coverage sensor node set to detect if it's a boundary or an inner node. Therefore, with existing false distances between the nodes, the coverage set becomes incomplete, which causes many inner nodes to declare themselves as boundary nodes. Note that increasing the average node degree, implies that the boundary nodes remain the same under the three different distances.

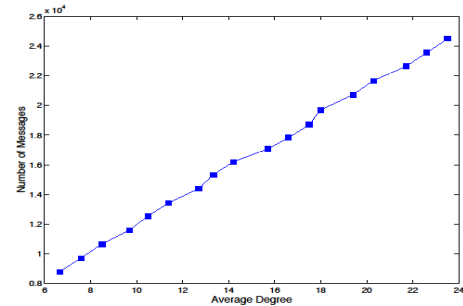
The reason is that with good average node degree, the coverage set of each sensor node will be adequate to provide a true declaration. The performance of our algorithm is not affected by the faulty distances among connected sensor nodes and the classification phase.

In the second test, we evaluate the communication overhead of the proposed algorithm as each boundary sensor node exchanges messages with its neighbor nodes to detect its

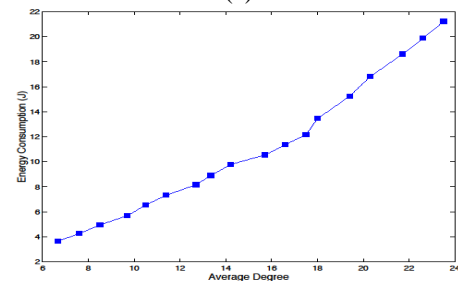
boundary neighbors or to select new nodes to be new boundary neighbors.

Figure 2a illustrates that the number of exchanged messages increases as the average node degree increases. In order to measure the energy dissipation of nodes, we use the same energy parameters and radio model as discussed in [26], which indicates that the transmission energy consumption is:

$$E_{Tx}(k, d) = \begin{cases} E_{elec} \times k + k \times \epsilon_{friss-amp} d^2 & \text{if } d < d_{crossover}, \\ E_{elec} \times k + k \times \epsilon_{two-ray-amp} d^4 & \text{if } d \geq d_{crossover}, \end{cases} \quad (1)$$



(a)



(b)

Figure 2. (a) Exchanged messages vs. average node degree, (b) Energy consumption vs. average node degree.

The reception energy consumption is

$$E_{Rx}(k, d) = E_{elec} \times k. \quad (2)$$

Where E_{elec} is the energy consumed for the radio electronics, $\epsilon_{friss-amp}$ and $\epsilon_{two-ray-amp}$ for a power amplifier. Radio parameters are set as $E_{elec} = 50 \text{ nJ/bit}$, $\epsilon_{friss-amp} = 10 \text{ pJ/bit/m}^2$, $\epsilon_{two-ray-amp} = 0.0013 \text{ pJ/bit/m}^4$, $d_{crossover} = 87 \text{ m}$. Figure 2b shows the relation between the average node degree and the energy consumption. Note that increasing the average degree sensor node causes increase in energy consumption of the network because when the average degree of sensor nodes increases, the number of exchanged messages increases which increases the energy consumption.

In the third test, we vary the number of deployed sensor nodes from 500 to 3000 nodes with an increment of 500 nodes and the average node degree is fixed to 21 degree.

Figure 3a shows the number of boundary sensor nodes. The result demonstrates that when we increase the number of deployed nodes in the network, the number of boundary nodes is also increased. However, when the average degree of the sensor node is fixed the communication range of the deployed sensor nodes is decreased by increasing the density of the network, which means that the sensing ranges of the nodes will be decreased and many small uncovered areas in the network appear as holes. For these reasons, many nodes will be classified as boundary nodes. We also evaluate the communication overhead when the density of the network is increased. Figure 3b shows the number of exchanged

messages increases by increasing the number of deployed sensor nodes. There is a disconnection in the network, the combination process cannot connect these nodes that are on the perimeters of the cycles which leads to classify these nodes as boundary node.

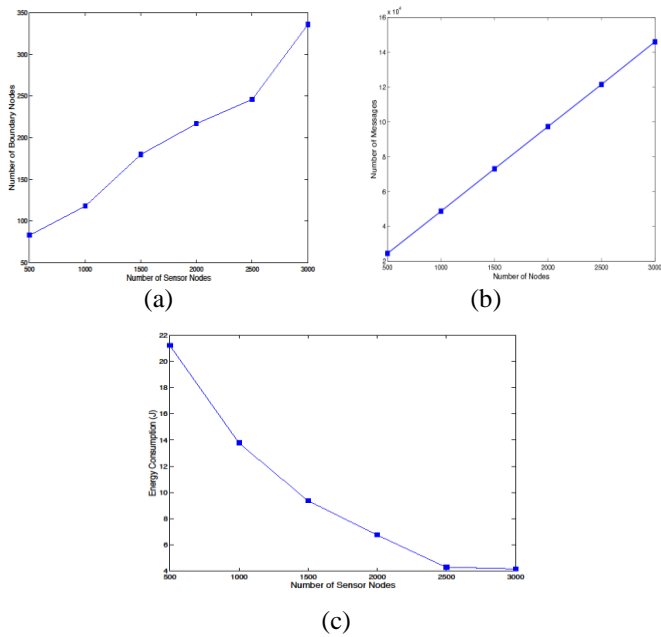


Figure 3. (a)Number of boundary nodes vs. number of deployed nodes in the network, (b)Number of exchanged messages vs. number of deployed nodes in the network, (c) Energy consumption vs. the number of deployed nodes in the network.

Figure 3c shows the energy consumption as the density of the network increases. The results show that the increase in the network density with fixed average degree leads to decrease in the energy consumption because the communication range of the sensor nodes decreases by increasing the density of the network. In summary, the boundary detection approach can identify all the boundary nodes of the network at low average node degree of 6.6 and high density of the network and can connect all the boundary nodes into sub-graphs and correctly classify each Sub-graph as an interior or exterior boundary of the network.

In the fourth test, we compare the simulation results of the proposed algorithm with existing BR algorithm [25]. 3500 sensor nodes are randomly deployed in monitoring regions of 400 m × 400 m and the average node degree is varied from 6 to 16 degree with an increment of 1.

Figure 4a shows the number of boundary nodes in BR and proposed algorithm. It shows that the number of boundary nodes decreases by increasing the average degree. In low average degree, the number of detected boundary nodes using our approach is smaller than the number of boundary nodes in BR because in our approach, each sensor node makes its decision locally and connects itself with the nearby boundary nodes if it detects that it represents a boundary node. While BR detects the boundary nodes by finding the chord-less cycles and then constructs the valid patterns by combining these cycles. Therefore, when there is a disconnection in the network, the combination process cannot connect these nodes that are on the perimeters of the cycles which lead to classify these nodes as boundary nodes.

In Figure 4b, the number of exchanged messages in BR is much bigger than the number of exchanged messages in our proposed algorithm because in BR, the number of exchanged messages between nodes to gather data and construct the valid patterns phase is very large.

However, in our algorithm, the sensor node in WSN makes its decision locally and only needs to exchange messages with its neighbors to decide. Also, in the connection phase of our algorithm, the sensor node exchanges about 3 messages with its boundary nodes to connect itself in the boundary sub-graphs.

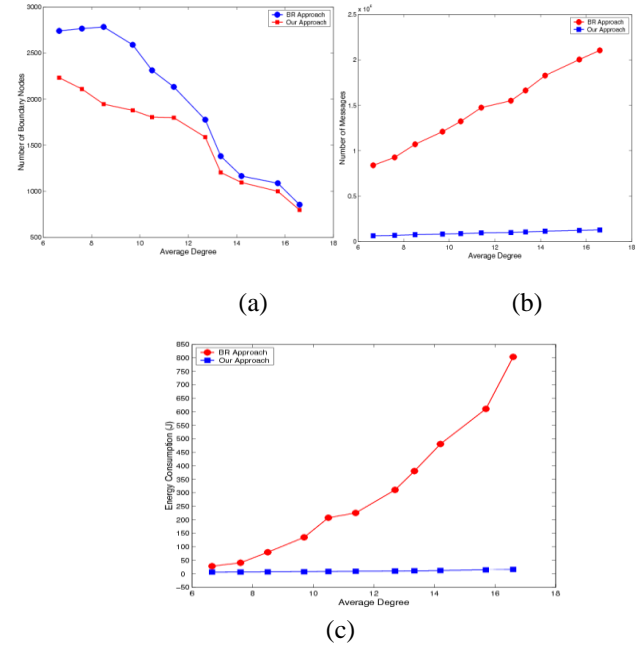


Figure 4. (a)Number of boundary nodes in BR and the proposed algorithms with different average node degrees, (b) Exchanged messages in BR and our proposed algorithms, (c) Energy dissipation in BR and our proposed algorithms.

Figure 4c shows the energy consumption in BR and the proposed approach. Since the number of exchanged messages in BR algorithm is much larger than the number of exchanged messages in the proposed approach this makes the consumed energy in BR much more than the consumed energy in the proposed approach. We can note that the energy dissipation at an average degree of 10.5 using our algorithm is only 4 J, while it is 180 J in BR.

In summary, our approach can detect the boundary nodes in low average node degree of 6.6 and connect them into different sub-graphs. The number of exchanged messages and consumed energy in our approach is much smaller than exchanged messages and consumed energy in BR.

5. Conclusion

In this paper, we have proposed a distributed algorithm to detect the boundary nodes in a WSN under the absence of any location information of nodes. Our algorithm can handle nodes that have heterogeneous sensing ranges. Our algorithm can successfully detect all the boundary nodes of the network or around the holes inside the network. All the boundary nodes of the network are formed as sub-graphs. We also proposed a new technique that correctly classified the different boundary subgraphs. Our simulation results show that our algorithm is efficient and scales well with different numbers of deployed nodes, improves the energy and

reduces the number of boundary nodes over existing algorithms.

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